

CS204

Fall 2017, Assignment #4

Problem 1.

5 + 2 pts

Fill out corresponding blocks. Then give your opinion: What is more important between CPU speed improvement and algorithm time complexity improvement?

input size(n)	Running time(sec)		
	$10^{-9}2^n$	$10^{-3}n^3$	$10n \log_2 n$
2			
8			
16			
32			
64			

Problem 2.

2 + 2 + 2 pts

In Chapter 3.1 Example 6, there is Algorithm 6: Greedy change-making algorithm. It tries to minimize the number of coins to return the change in greedy sense: given coins for each type $c_1 < \dots < c_n$, use one coin c_i to change k satisfying $c_i \leq k < c_{i+1}$, and re-run the process with change $k - c_i$ until changes becomes 0.

- Suppose we have infinitely many coins for each type: 100 cents, 50 cents, 10 cents, 5 cents, and 1 cent. Using that algorithm, describe how to change 486 cents.
- Suppose that now we have infinitely many coins for each type: 120 cents, 100 cents, 20 cents, 5 cents, and 1 cent. Using that algorithm, describe how to change 327 cents.
- Does b) gives a minimized number of coins as a solution? If not, give a better solution.

Problem 3.

3 + 2 + 3 + 2 + 1 + 1 pts

Fix $N = 2^n$ for some $n \in \mathbb{Z}^+$. Your task is to sort an integer array A with size N : $A[0, \dots, N - 1]$ in ascending order.

- Construct a function that takes an integer array arr , integers $start, mid, finish$, and then sort $arr[start, \dots, finish - 1]$. Assume that $arr[start, \dots, mid - 1]$ and $arr[mid, \dots, finish - 1]$ are already sorted in ascending order, and also assume that change of the parameter arr will be automatically applied to the caller.
- Now suppose $A[0, N/4 - 1], A[N/4, N/2 - 1], A[N/2, 3N/4 - 1], A[3N/4, N - 1]$ are already sorted in ascending order. What acts you have to do to get a fully sorted A ? Answer using your function in a).
- Using the idea of b) and the function constructed in a), describe the algorithm to sort an unsorted array A , starting from sorting 2-element $N/2$ arrays. You would have to use the iterative loop: start from parameter = 2 and double it step by step.
- The function in a) will compare elements in array at most $finish - start$ times. Count the upper bound of the number of comparisons to sort A fully and answer using n .
- Convert the answer in d) using N instead, and then give a time complexity of the algorithm using big-O notation.
- Compare the time complexity with bubble sort.